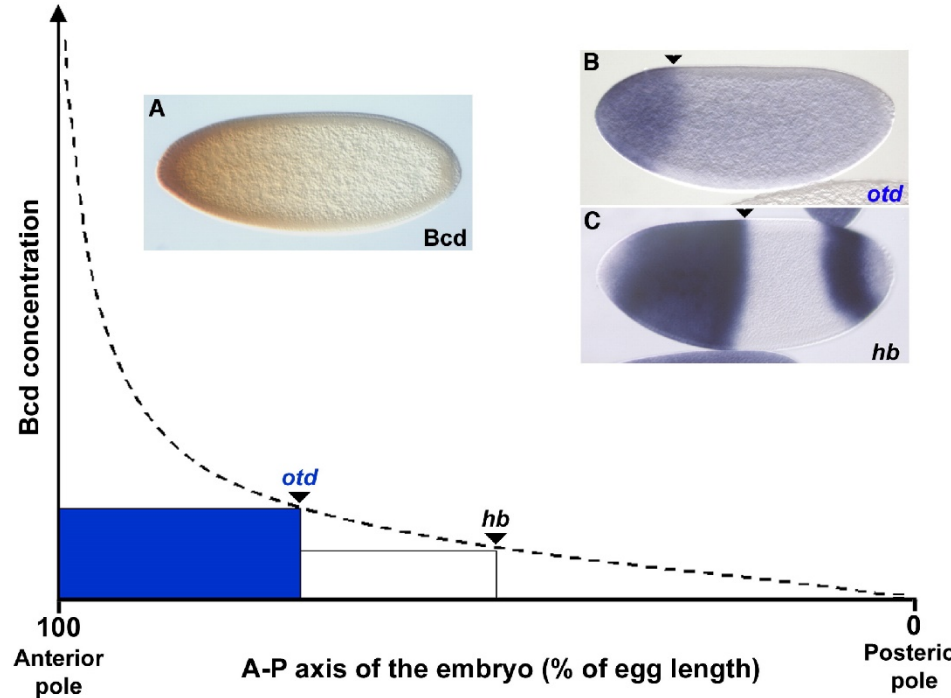
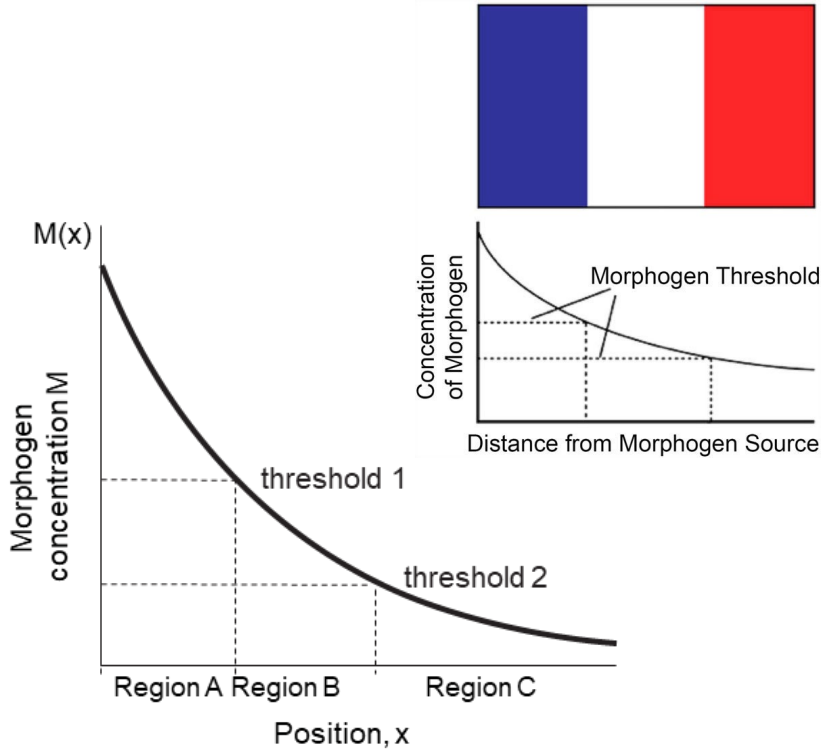
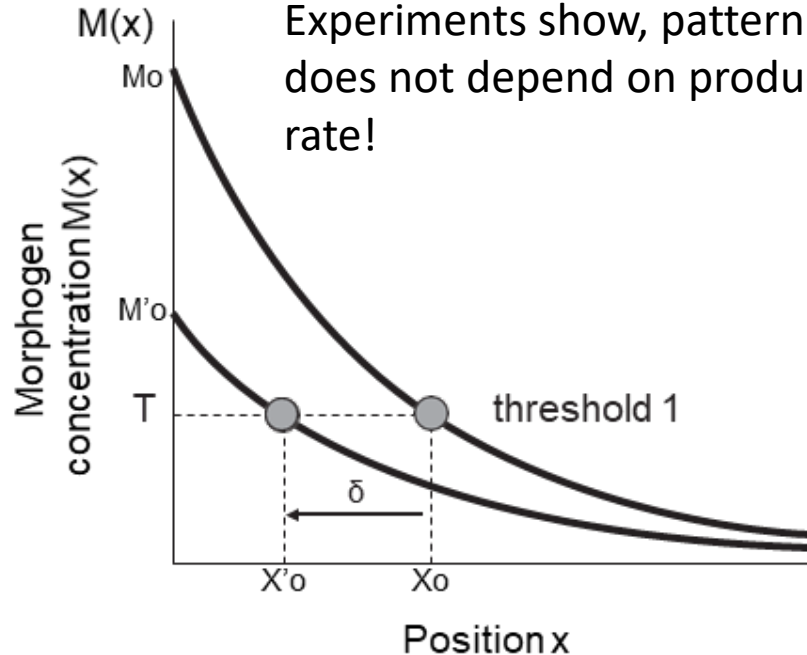


# Robust Patterning in Development



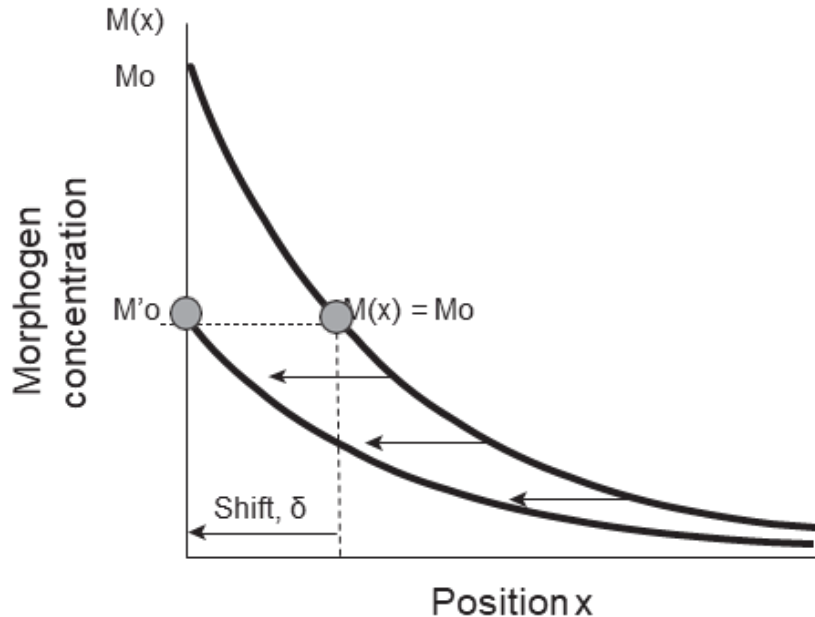
Question how can the position be independent of protein production?



Experiments show, patterning does not depend on production rate!

Why the diffusion does not explain this!

General feature: Shift is always the same!!! Independent of position



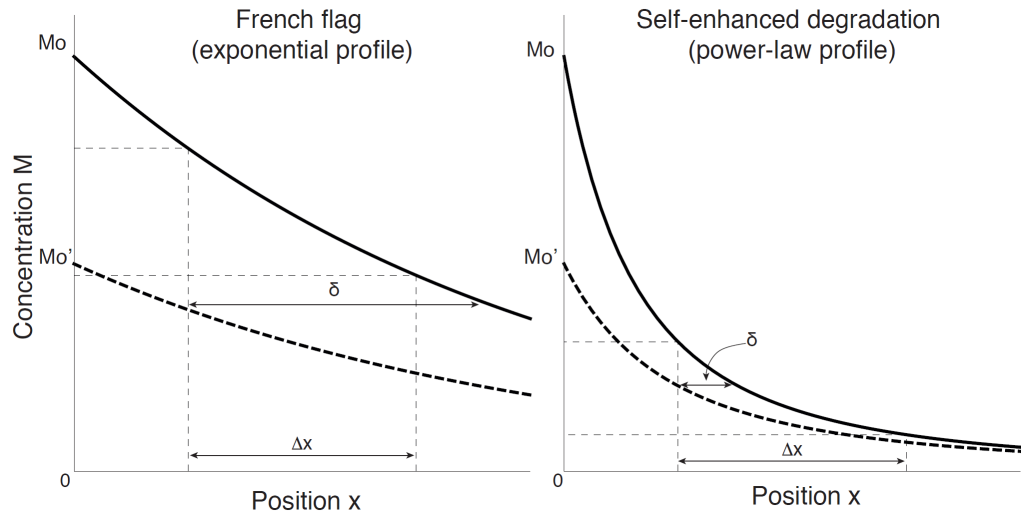
Problem: Pattern with long range AND high robustness!

Needs two properties:

- 1) Fast decay at  $x=0$  (robustness against  $M_0$ )
- 2) Slow decay at large  $x$ , to increase effect of  $M$

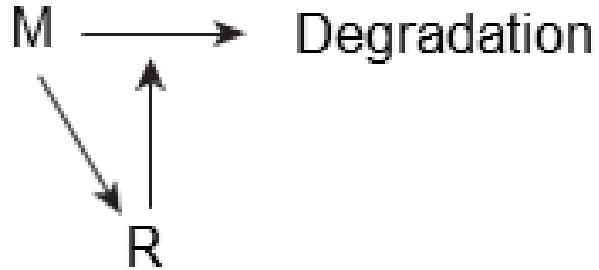
# Exponential decay does not work, maybe nonlinear decay function?

$$M = A (x + \varepsilon)^{-2} \quad \varepsilon = (\alpha M_o / 6 D)^{-1/2} \quad A = 6 D / \alpha$$



Self enhanced degradation is possible mechanism that solves the puzzle

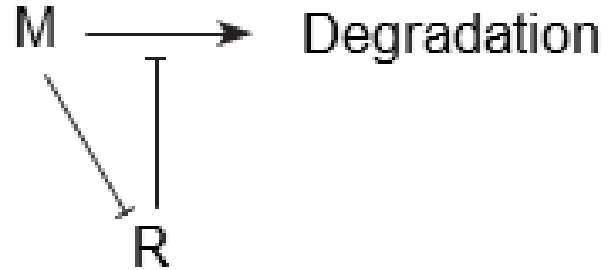
a



Receptor stimulates degradation (endocytosis)

Example: Hedgehog (M) and Patched (R)

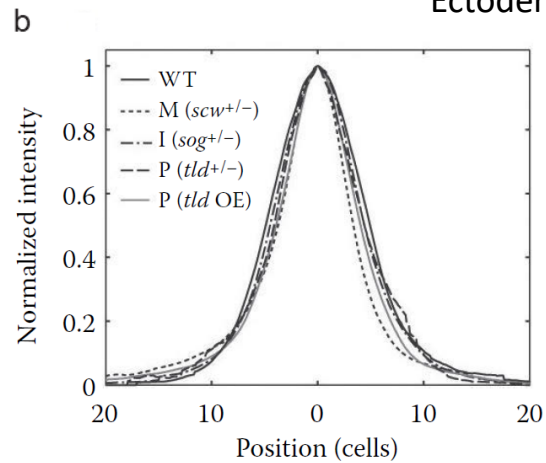
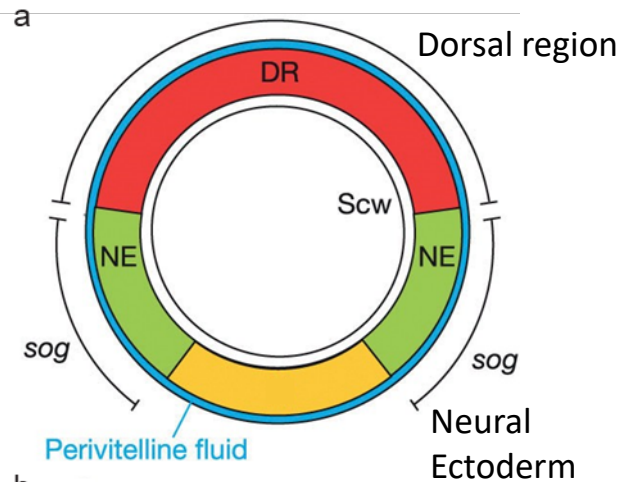
b



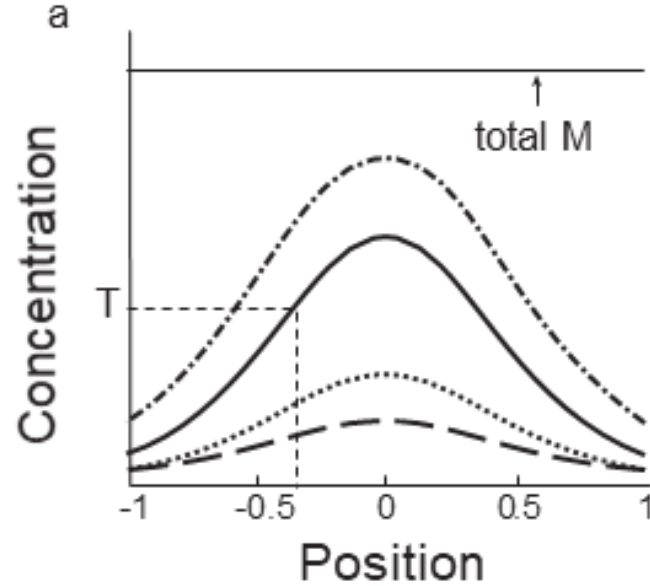
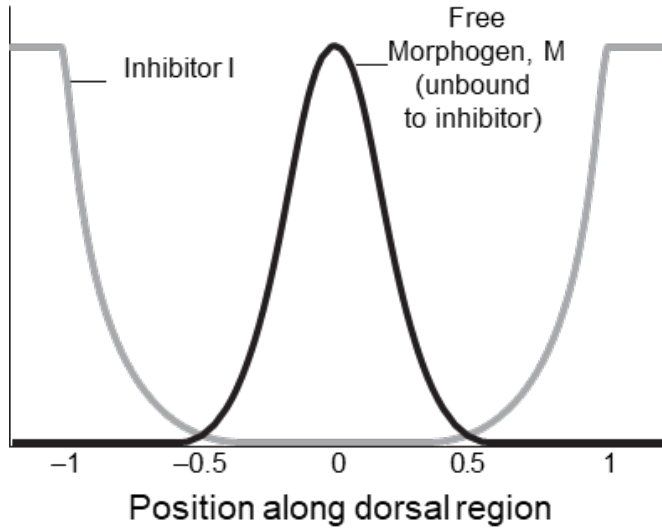
Receptor suppresses degradation (suppression of protease)

Example: Wingless (M) and Frizzled (R)

## Robust patterning as principle to find right mechanism

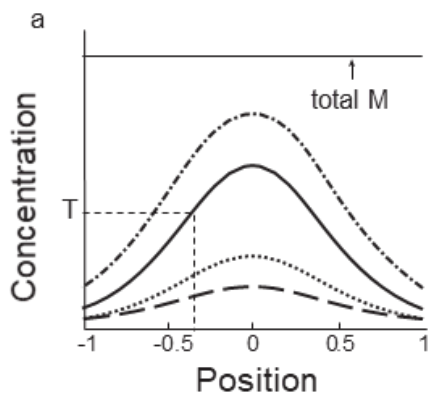


Simplest approach: I degrades M everywhere but not in the DR

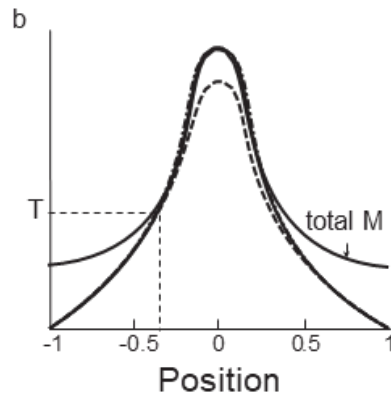


Problem: Not robust against changes in M, I and P

Hmm, self enhanced degradation does not work (I is degraded, not M!)



Only numerical model for full  
Deq, but of these 97% non-  
robust



0.5% of solution highly robust  
with powerlaw!

Single calls where:

- M could not diffuse freely,  
only in the complex  
( $D_c \gg D_m$ )
- I is not degraded by P unless  
in complex. ( $\alpha_c \gg \alpha_i$ )